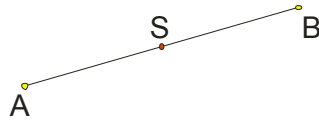


# CENTRAL SYMMETRY

Draw along. Let the S be its central point.



It is clear that  $AS = BS$ .

Points A and B are symmetric to S. S is centre of symmetry.

For points A and B say that they are symmetric with respect to point S. Point S is the center of symmetry.

More can be said that the point A to point B symmetric relative to point S, ie that B is symmetric with respect to A in S.

**Mapping of each point A and some planes  $\alpha$  translates into a point  $A'$  which is symmetric to the point A in relation to the point S with the plane  $\alpha$ , called the central plane of symmetry  $\alpha$  with center in S**

Central symmetry is usually marked with  $I_S$ , of course, if your teacher marks it differently and you do so...

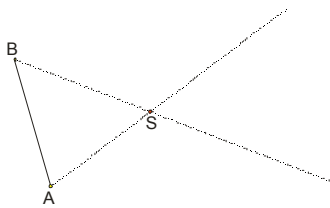
If you are not confused, **axisymmetry** is similarly marked  $I_s$ , with a team that was down slightly in the index letter s.

For figure F from plane  $\alpha$  we say that maps in figure  $F'$  is central symmetry  $I_S$  if each point of A figure F match point with a figure  $A'$  figure  $F'$  is a central symmetric point A:  $A' = I_S(A)$  and vice versa.

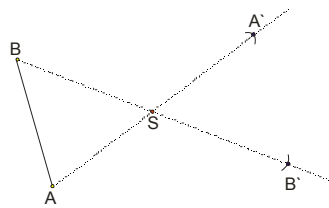
**Example 1.**

Along AB is given. Construct along the central symmetry if the center of symmetry, the point S, no longer belongs.

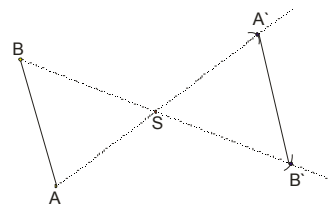
**Solution:**



picture 1.



picture 2.



picture 3.

Merge vertices given long with a center of symmetry S and extend to the other side ... (picture 1)

Sting compass point in S, we take the distance to A (ie SA) and move, we got a point  $A'$ , and also to perform to point B, then the distance SB switch to another page and get  $B'$  (picture2)

Obtained merge point  $A'$  and  $B'$ , we get (Along)  $A'B'$ , which is centrally symmetric to AB in relation to the point S (picture3)

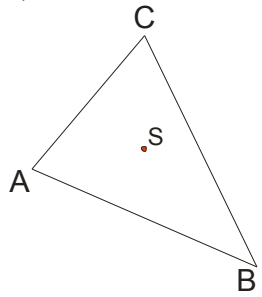
**Example 2.**

Construct a triangle  $A'B'C'$  centrally symmetric to given triangle  $ABC$  if the center of symmetry:

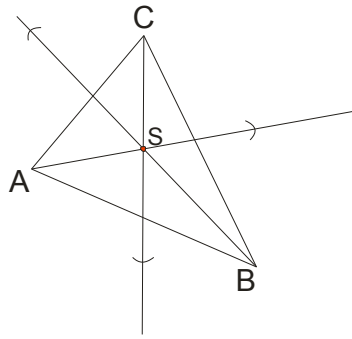
- a) within the triangle
- b) outside the triangle

**Solution:**

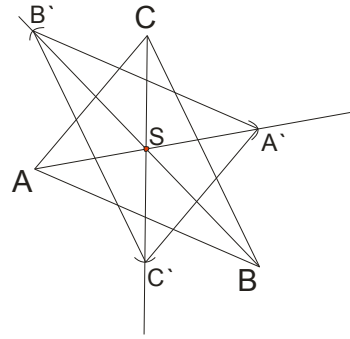
a)



picture 1.



picture 2.



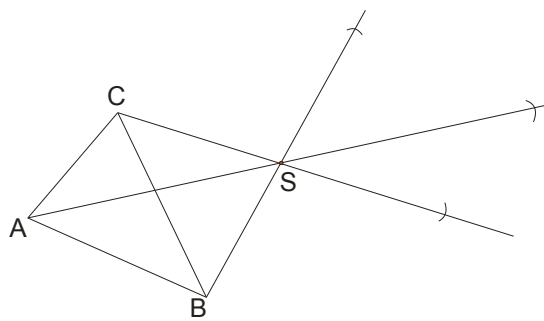
picture 3.

Choose a point inside a triangle with (arbitrary), we can see in picture 1.

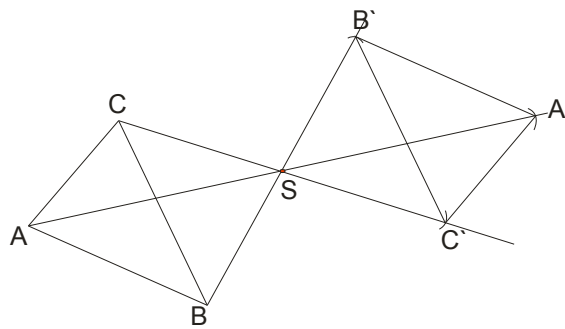
Merge the vertices of a triangle with the center of symmetry S and continue ... We have three lines. Thrust compass point in S and transmits the distance to A, B and C on the other hand the corresponding lines. (picture 2.)

Merge points, and obtained our required triangle  $A'B'C'$ , which is centrally symmetric to the given triangle  $ABC$  to the point S is inside the triangle.

b)



picture 1.



picture 2.

The procedure is analogous as under a) with only a point outside the triangle we choose arbitrarily

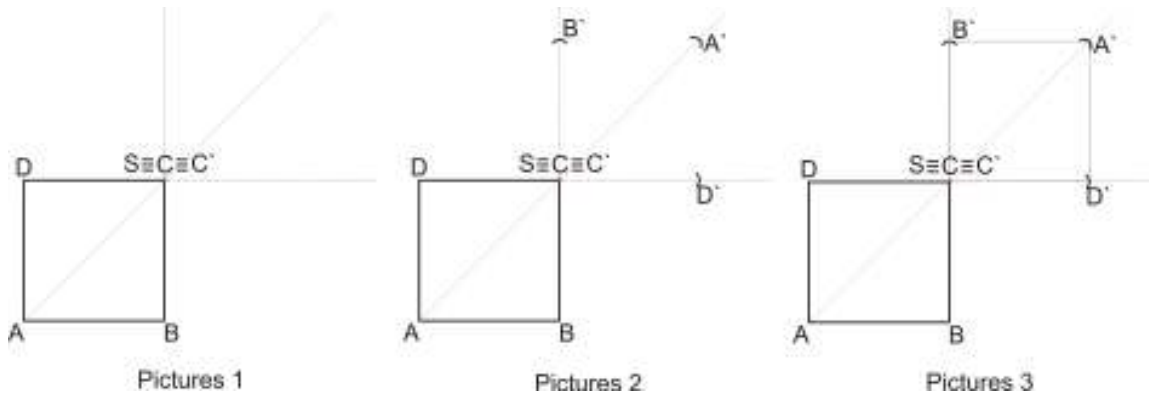
**Example 3.**

**Construct a square with  $A'B'C'D'$  centrally symmetric given square  $ABCD$  if the center of symmetry:**

- a) vertices  $C$
- b) on  $BC$

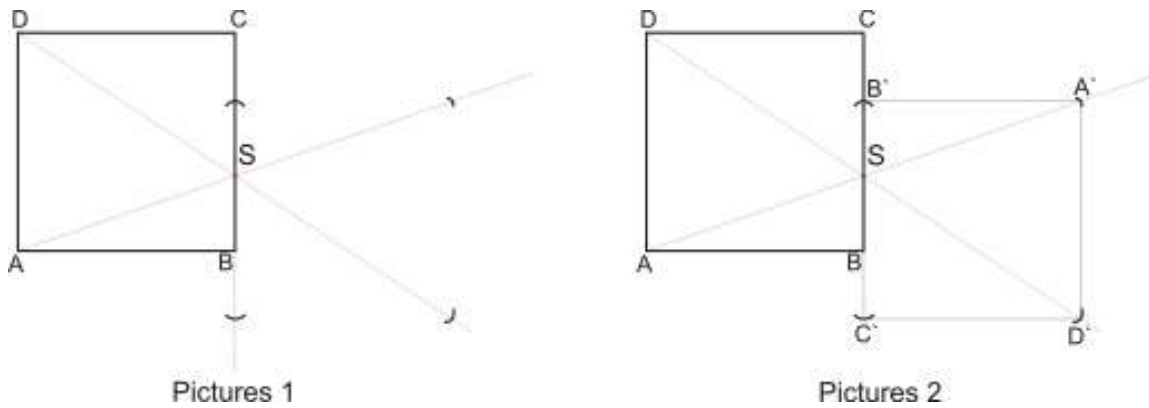
**Solution:**

a)



As specified the topics  $C$  center of symmetry, that is what your image at the same time, that is, for  $C \equiv C'$ , for the other points do the procedure...

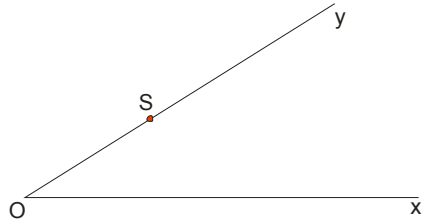
b)



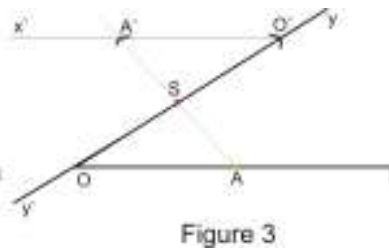
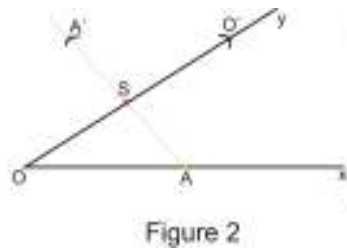
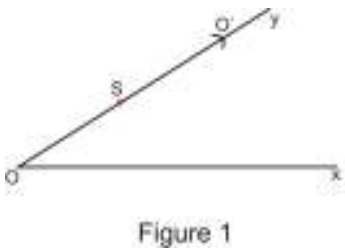
Arbitrarily choose a point  $S$  on  $BC$  and we do everything according to procedure...

**Example 4.**

**Given angle of  $\angle xOy$  transferred central symmetry with respect to point S (see picture)**



**Solution:**



First, move threads of the angle (Figure 1)

To switch arm of Ox, we will take an arbitrary point A on the arm and move it ... (Figure 2)  
merge O `A` and thus get arm O `x` (Figure 3)

**Example 5.**

To rounds, are given,  $k$  i  $k_1$ , but with different centers  $O$  and  $O_1$ , which are cut. Through one of the points of intersection withdraw the right circle that  $p$  these circles cut the same tendon leader.

**Solution:**

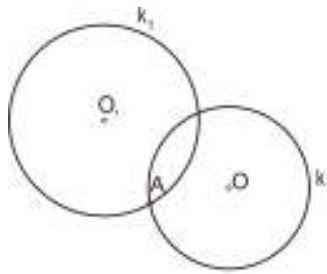


Figure 1

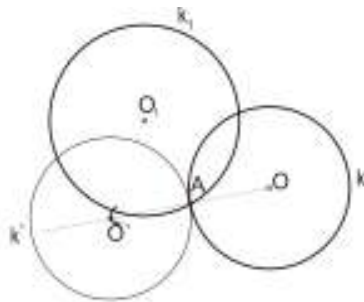


Figure 2

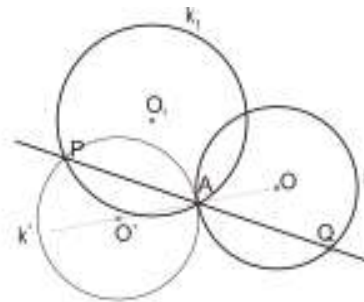


Figure 3

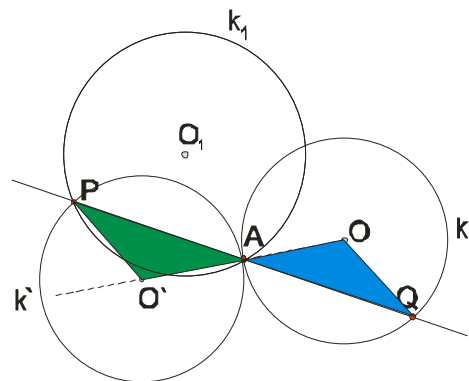
**In Figure 1 We draw two given circles and marked with A single point of intersection of their circle.**

The idea is that we map the central  $k$  symmetry circle compared to point A. To have it done it is enough to map the centre of O the circle  $k$ , and the radius will, of course, remain the same. (Figure 2)

The intersection of the circle obtained  $k'$  the circle  $k_1$  gives us the point P. we pull a line right through the points A and P, we get point Q on the circle  $k$ . **Tendon PA and QA su jednake.** (Figure 3)

**Why?**

Recognize triangles APO` and AOQ.



**These two triangles are matched, so PA=AQ.**